

Current research: Ian

INFO/STSCI/ILRST 3900: Causal Inference

28 Nov 2023

# Learning goals for today

At the end of class, you will be able to

1. define effects when some potential outcomes do not exist
2. estimate by bounding
3. connect ideas from this class to current research

# Non-existent outcomes in research on inequality

A causal approach

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Replication  
code [here](#)

Try our (beta) R package!  
[ilundberg.github.io/pstratreg](https://ilundberg.github.io/pstratreg)

# The setting

Parenthood reduces hourly wages for women

(Budig & England 2001; Gough & Noonan 2013)

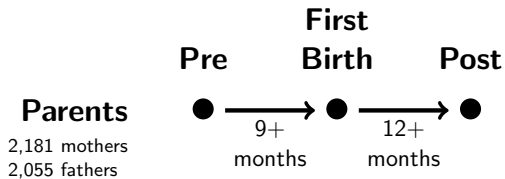
and increases wages for men

(Killewald 2013; Yu & Hara 2021)

The motherhood wage penalty may be disappearing over time

(Pal & Waldfogel 2016; Buchmann & McDaniel 2016; but see Jee et al. 2019)

Data: NLSY97



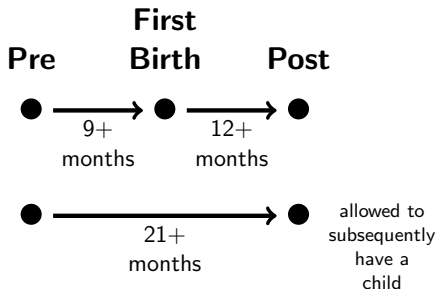
# Data: NLSY97

## Parents

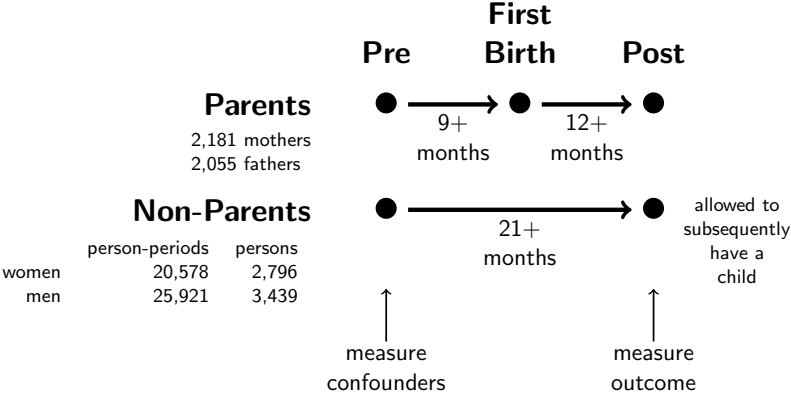
2,181 mothers  
2,055 fathers

## Non-Parents

	person-periods	persons
women	20,578	2,796
men	25,921	3,439



# Data: NLSY97



$$\begin{aligned}\log(\text{Wage}) = & \beta_0 + \beta_1(\text{Mother}) \\ & + \beta_2(\text{Age}) \\ & + \beta_3(\text{Married}) \\ & + \beta_4(\text{Education}) \\ & + \beta_5(\text{Work Experience}) \\ & + \beta_6(\text{Full-Time}) \\ & + \beta_7(\text{Tenure in Job}) \\ & + \epsilon\end{aligned}$$




Maya



# Maya

	<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
employment		—		=	
wage		—		=	



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wage		—		=	



# Maya

	<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
employment		—		=	0
wage		—		=	



# Maya

	<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
employment		—		=	0
wage	\$30	—		=	

# Maya

	<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
employment		—		=	0
wage	\$30	—	\$40	=	

# Maya


	<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
employment		—		=	0
wage	\$30	—	\$40	=	-\$10





# Mia

	<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
employment		—		=	
wage		—		=	



# Mia

	<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
employment	<del></del>	—		=	
wage		—		=	



# Mia

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wage	??	—	\$20	=	

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	<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
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employment	<del></del>	—		=	-1
wage	??	—	\$20	=	??

## Principal Stratification

Frangakis & Rubin 2002; Zhang & Rubin 2003

For an intro, see Miratrix et al. 2018



## Maya

if a mother    -    if not    =    effect



-



=

0

\$30

-

\$40

=

-\$10

## Mia

if a mother    -    if not    =    effect



-



=

-1

??



-

\$20



=

??



## Maya

<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
	—		=	0
\$30	—	\$40	=	-\$10


## Nancy

<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
	—		=	0
\$30	—	\$40	=	-\$10



## Mia

<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
<del></del>	—		=	-1
??	—	\$20	=	??


## Nia

<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
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## Maya is a Mother

<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
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\$30	—	\$40	=	-\$10

## Nancy is a Non-Mother

<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
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DROPPED



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## Average Observed

\$30

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**DROPPED**

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<del></del>	-		=	-1
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**Average Observed**

\$30



**Average Observed**

\$30



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1) Average effect of motherhood on employment

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\$30	—	\$40	=	-\$10

## Mia is a Mother

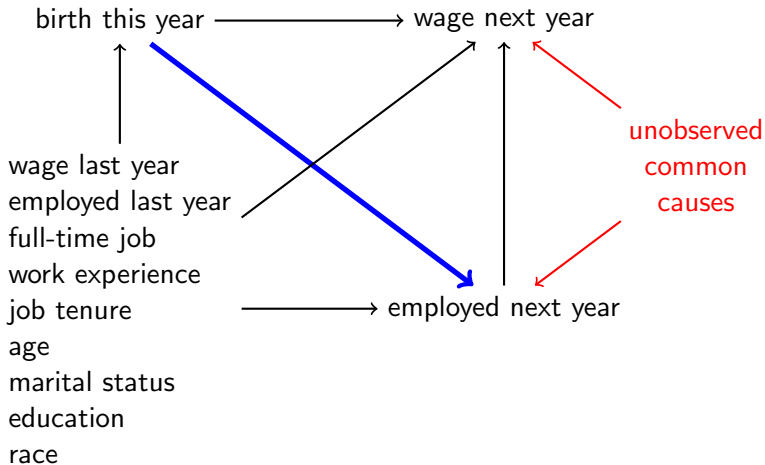
<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
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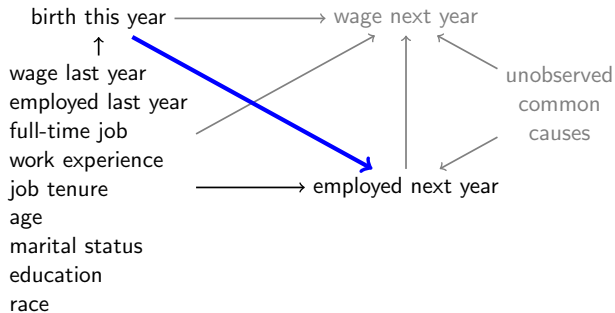
<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
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- 1) Average effect of motherhood on employment
- 2) Wage effect among those employed regardless

# Causal assumptions

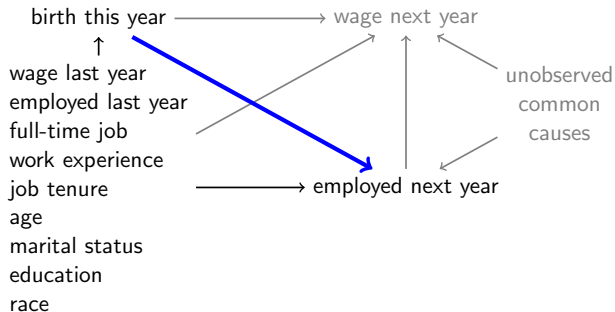


# Estimation: Effect on employment



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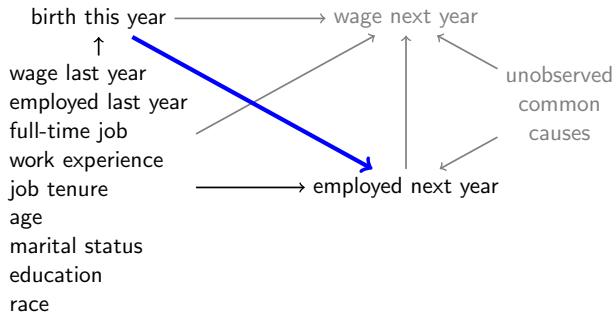
Model employment given birth and confounders



# Estimation: Effect on employment

Model employment given birth and confounders

1) recode birth as TRUE. Predict for everyone

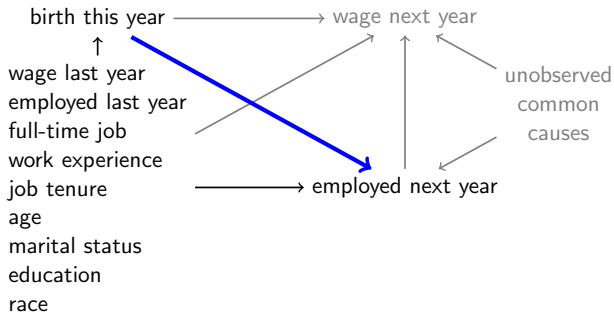


# Estimation: Effect on employment

Model employment given birth and confounders

1) recode birth as TRUE. Predict for everyone

2) recode birth as FALSE. Predict for everyone



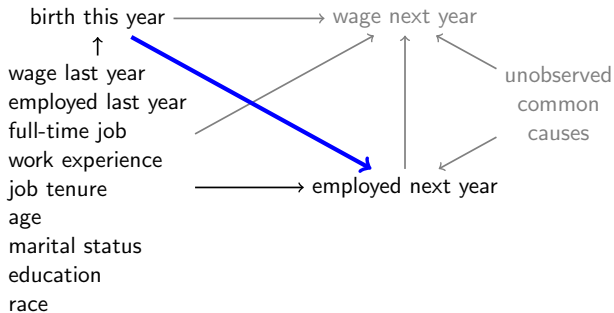
# Estimation: Effect on employment

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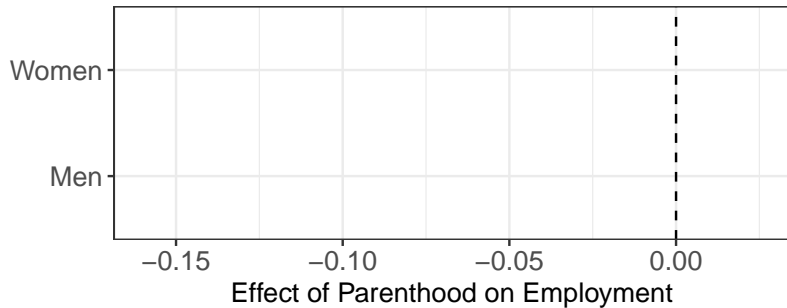
2) recode birth as FALSE. Predict for everyone

average (1) – (2) among the mothers

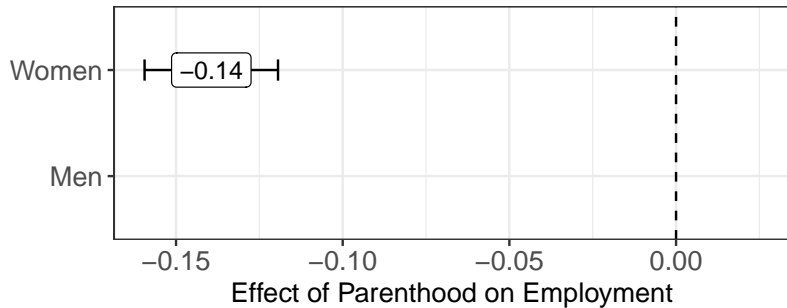




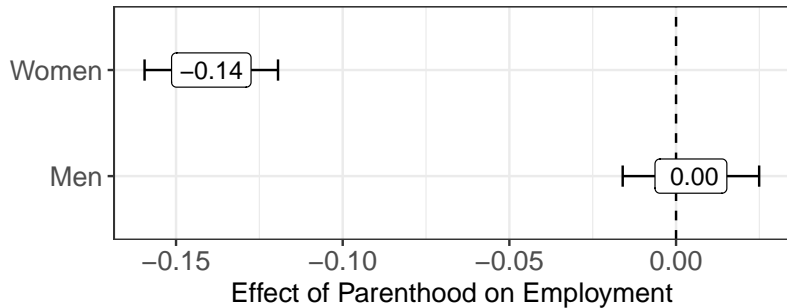
## Results: Effect on employment



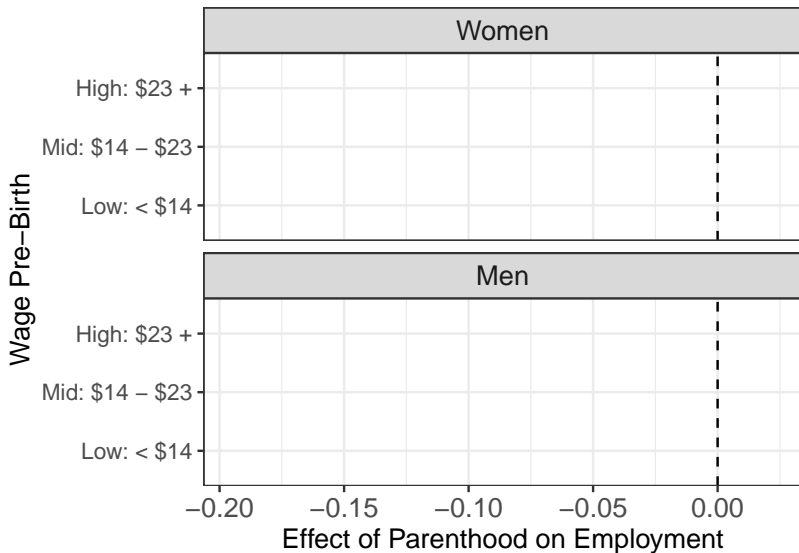
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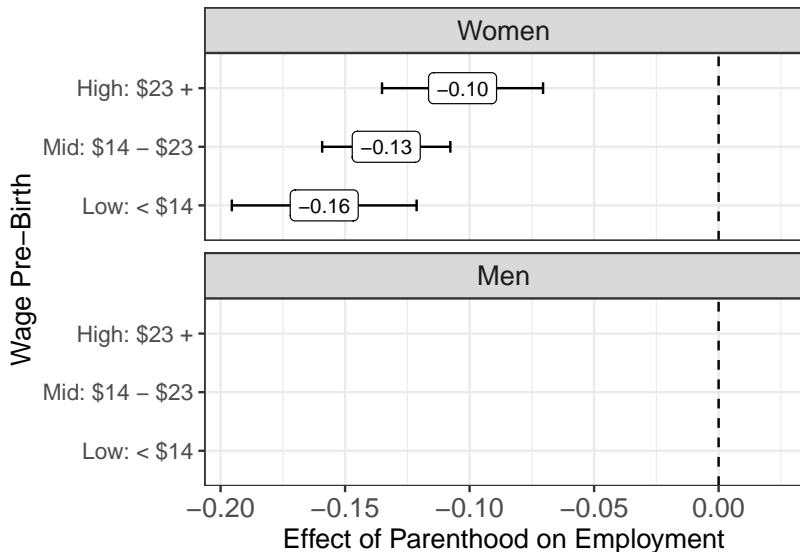
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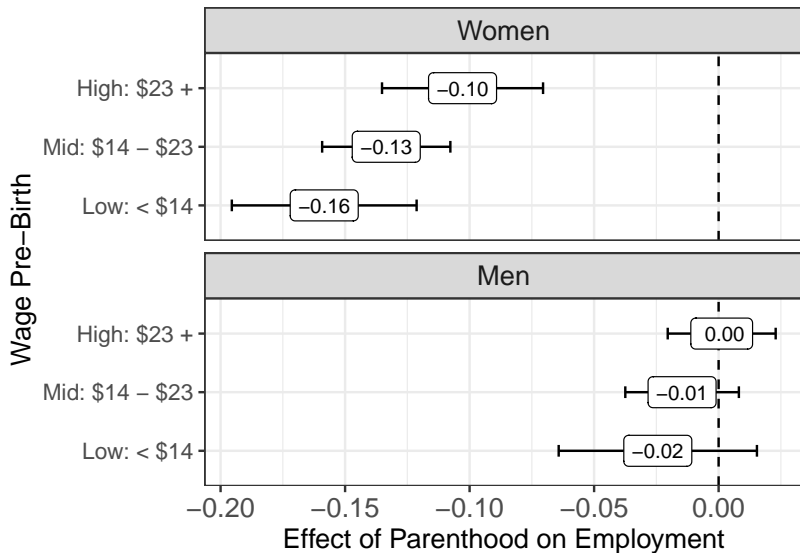
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## Results: Effect on employment





## Results: Effect on employment





## Maya is a Mother

<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
	—		=	<b>0</b>
\$30	—	\$40	=	-\$10


## Nancy is a Non-Mother

<u>if a mother</u>	—	<u>if not</u>	=	<u>effect</u>
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## Mia is a Mother



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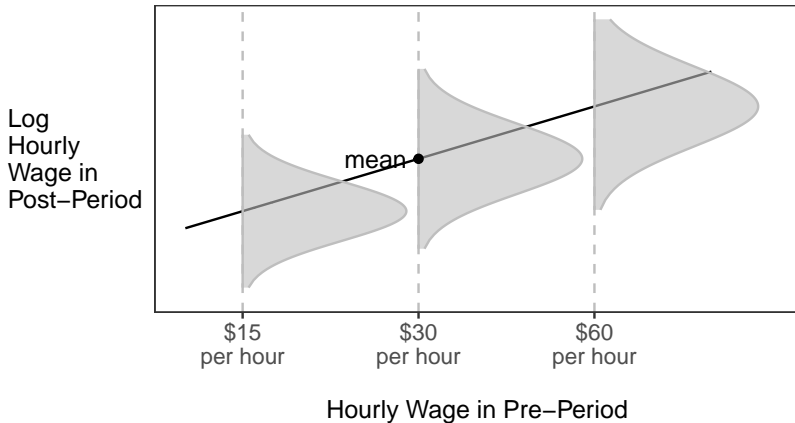
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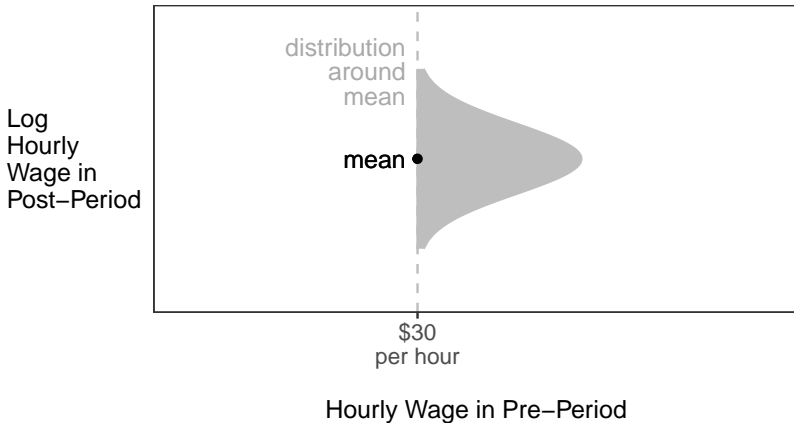
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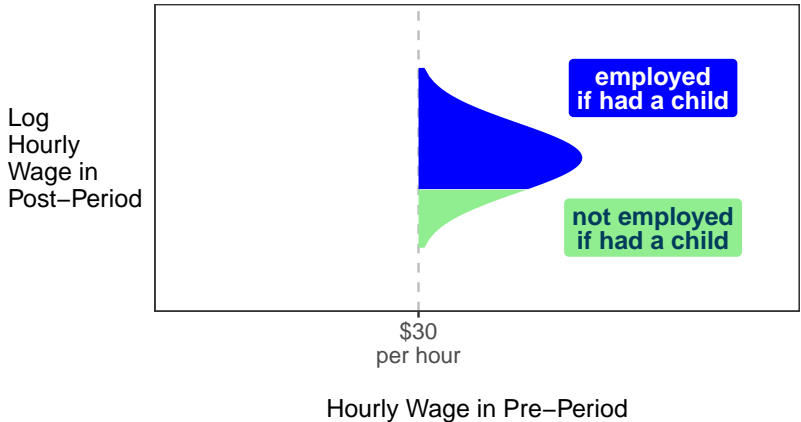
## Wages of Employed **Non-Mothers**



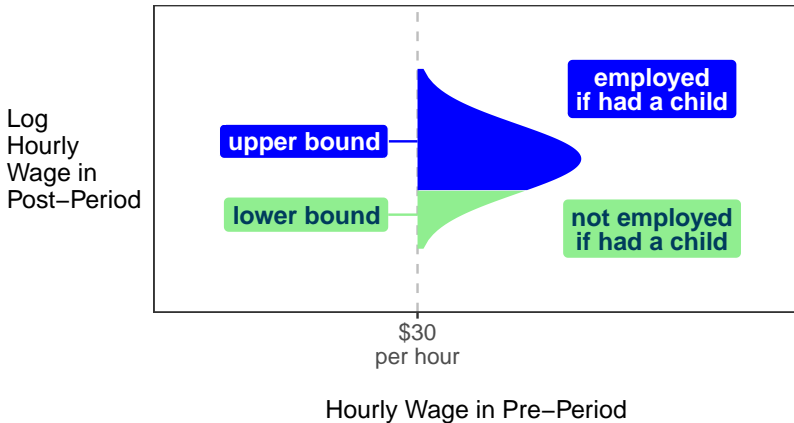
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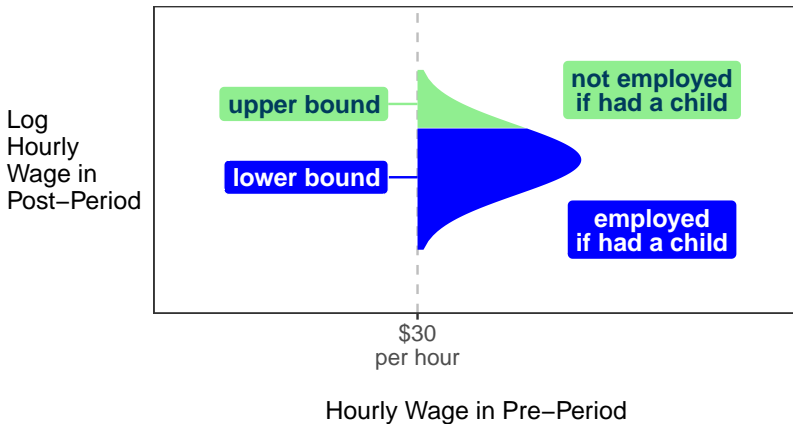
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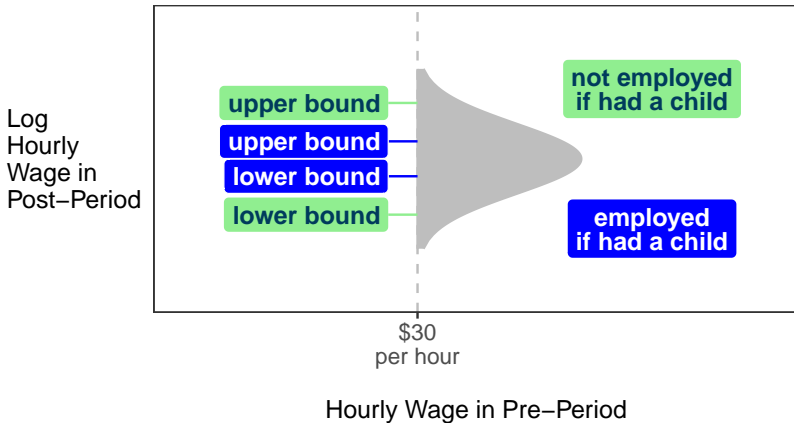
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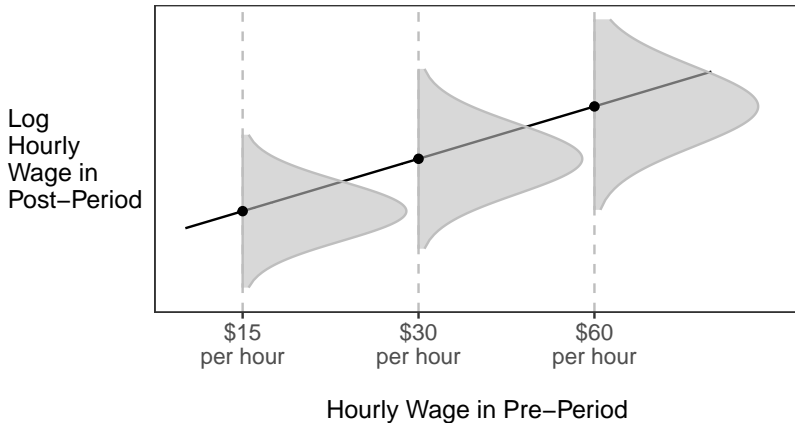


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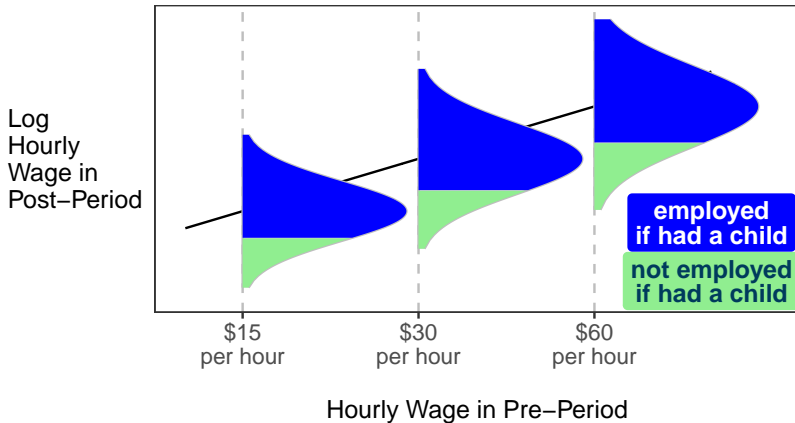




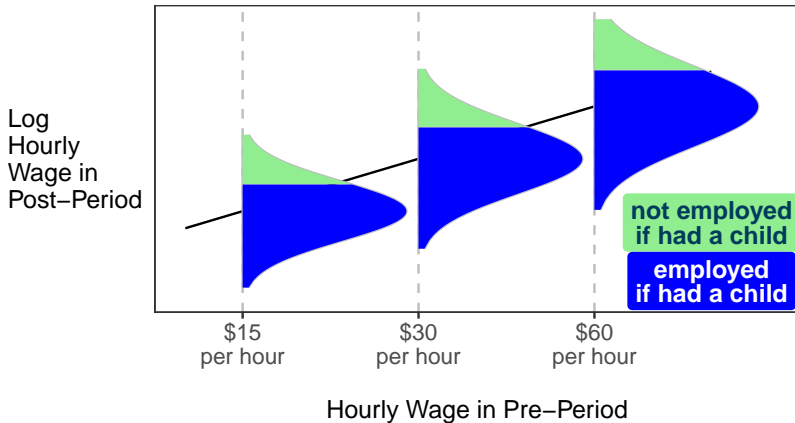
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## Wages of Employed **Non-Mothers**



bound  
this  
↓

Log wage of **as a mother** – **as a non-mother**

among those who would be employed in either condition

bound  
this  
↓

Log wage of **as a mother** – **as a non-mother**

among those who would be employed in either condition

### **Assumption**

Employed mothers would also be employed  
if they had no children

simple  
mean  
↓

bound  
this  
↓

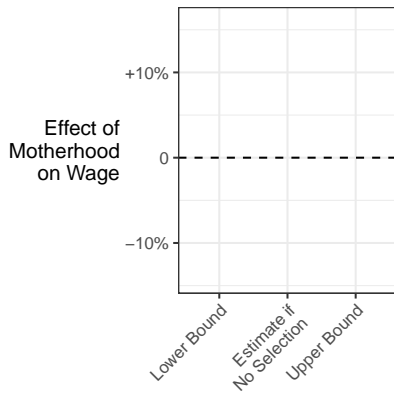
Log wage of **as a mother** – **as a non-mother**

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### Assumption

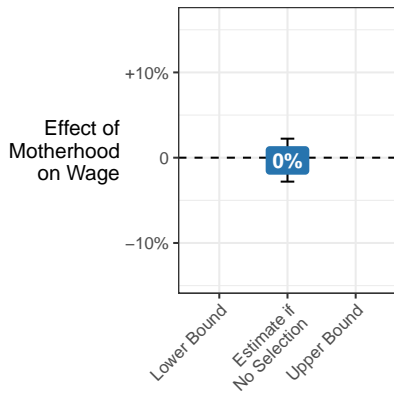
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# Results



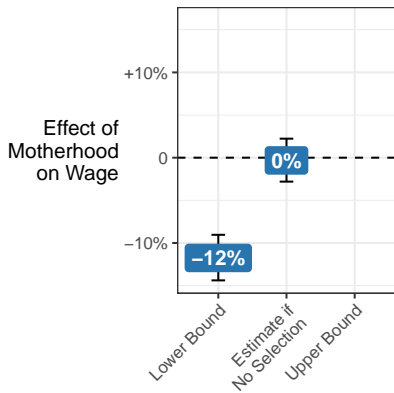
# Results

Employed Mothers — Employed Non-Mothers

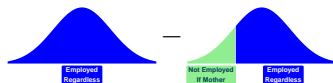




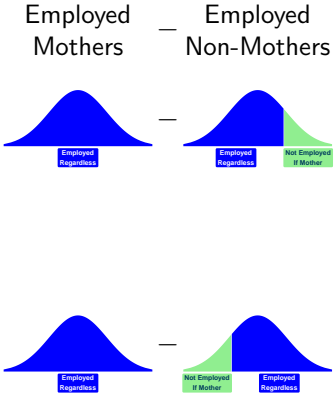
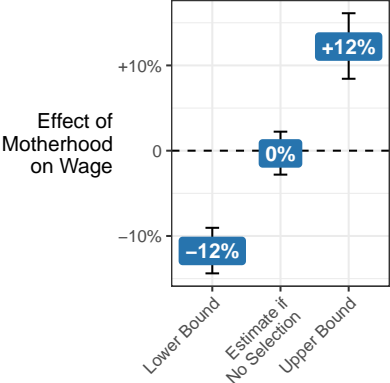
# Results



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# What we know that we did not know before

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in recent years, motherhood only weakly predicts pay\*

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**or**

2. employed non-mothers are the wrong comparison population

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1. motherhood's causal effect on pay is small

**or**

2. employed non-mothers are the wrong comparison population

▶ lowest-earning non-mothers might stop paid work with a child



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$$\begin{array}{r} \text{~~☑}~~ \\ \text{??} \end{array} - \text{☑} = -1$$
$$\text{??} - \$25 = \text{??}$$

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$$\cancel{\text{Briefcase}} - \text{Briefcase} = -1$$
$$?? - \$25 = ??$$



## pstratreg: An R package

<input type="text" value="Search"/>	
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pstratreg (pstratreg)

R Documentation

## Estimate Principal Stratification Regression Bounds

### Description

Uses principal stratification and parametric models to bound the average causal effect among those who would have a valid outcome under either treatment condition

### Usage

```
psratreg(  
  formula_y,  
  formula_m,  
  family_y = "gaussian",  
  homoskedastic = T,  
  data,  
  weights = NULL,  
  treatment_name,  
  monotonicity_positive = FALSE,  
  monotonicity_negative = FALSE,  
  aggregate = TRUE,  
  group_vars = NULL  
)
```

# Learning goals for today

At the end of class, you will be able to

1. define effects when some potential outcomes do not exist
2. estimate by bounding
3. connect ideas from this class to current research