

# Conditional Exchangeability in Observational Studies

INFO/STSCI/ILRST 3900: Causal Inference

17 Sep 2024

# Logistics

- ▶ Peer reviews for pset 1 due today by 5pm
- ▶ Pset 2  $\longrightarrow$  Due Tue (9/24) @ 5pm
- ▶ Post questions on [Ed Discussion](#) or come to office hours!
- ▶ After class, read 3.4 and 3.5 of [Hernán & Robins](#)

# Learning goals for today

At the end of class, you will be able to:

1. Explain the challenge of satisfying conditional exchangeability in observational data
2. Explain part one the consistency assumption
  - ▶ Well-defined, precise treatments

## Check Your Understanding: Exchangeability

*Discuss in groups, then submit your response individually to PollEverywhere. Your response won't be graded.*

Recall the of definition (marginal) exchangeability:

$$Y_i^{a=1}, Y_i^{a=0} \perp\!\!\!\perp A_i$$

**If exchangeability holds, which of the following are true?**



<https://pollev.com/causal3900>

## Poll Everywhere: Possible Answers

Recall the of definition (marginal) exchangeability:

$$Y_i^{a=1}, Y_i^{a=0} \perp\!\!\!\perp A_i$$

**If exchangeability holds, which of the following must be true?**

- ✓ (A) Your potential outcome under treatment would be the same regardless of the treatment observed
  - ▶  $E(Y_{\text{You}}^{a=1} | A_{\text{You}} = 1) = E(Y_{\text{You}}^{a=1} | A_{\text{You}} = 0)$
- ~~(B)~~ Your potential outcome depends on what treatment is observed
- ✓ (C) Your potential outcome under no treatment would be the same regardless of the treatment observed
  - ▶  $E(Y_{\text{You}}^{a=0} | A_{\text{You}} = 1) = E(Y_{\text{You}}^{a=0} | A_{\text{You}} = 0)$
- ~~(D)~~ Your observed outcome depends on what treatment is observed

# Conditional Exchangeability in Observational Studies

- ▶ Conditional exchangeability lets us estimate causal effects
- ▶ Stratification: conditional average treatment effects
- ▶ Standardization or inverse probability weighting: population average treatment effect
- ▶ By design, conditional exchangeability holds in conditionally randomized experiments
- ▶ Conditional exchangeability more reasonable in observational data than marginal exchangeability

# What could go wrong?

- ▶ What does  $Y_i^{a=1}, Y_i^{a=0} \perp\!\!\!\perp A_i$  (exchangeability) mean?
- ▶ Effect of college degree (A) on income level (Y) at age 30
  - ▶  $A_i = 1$  if college degree,  $A_i = 0$  if no college degree
- ▶ Suppose we have information on parental income (L)
  - ▶  $L_i = 1$ : parents have high income
  - ▶  $L_i = 0$ : parents have low income
- ▶ L associated with the outcome  $L \not\perp\!\!\!\perp Y_i^{a=1}, Y_i^{a=0}$

# What could go wrong?

- ▶ Effect of college degree ( $A$ ) on income level ( $Y$ ) at age 30
  - ▶  $A_i = 1$  if college degree,  $A_i = 0$  if no college degree
- ▶ Suppose we have information on parental income ( $L$ )
  - ▶  $L = 1$ : parents have high income
  - ▶  $L = 0$ : parents have low income
- ▶  $L$  associated with the outcome  $L \not\perp Y_i^{a=1}, Y_i^{a=0}$
- ▶ Are your own education level and your parents' income the only two factors that influence your income level?
- ▶ What additional information would you gather to make conditional exchangeability plausible?

$$Y_i^{a=1}, Y_i^{a=0} \not\perp A_i \mid L_1, L_2, \dots, L_k$$



# Conditional exchangeability in observational data

- ▶ Even if gathering data was possible for every covariate we want, when do we stop?
- ▶ Never 100% sure that conditional exchangeability holds
- ▶ Is it reasonable?
- ▶ Causal inference with observational data requires expert knowledge!

# Identification Assumptions

- ▶ Exchangeability is an *identification assumption*
- ▶ Identification assumptions take us from observable quantities to causal effects (which deal with unobservable potential outcomes)
- ▶ In randomized experiments, often take identification assumptions for granted
- ▶ The rest of the class will mostly deal with observational settings!
- ▶ This means we have to think more critically about the implicit assumptions we often make

# Activity

- ▶ Looking at data to analyze the effectiveness of a medication on relieving headaches
- ▶ *“What is the effect of taking HeadacheRelief™ on a person’s headache within one hour of taking it?”*
- ▶ Info collected for each study participant:
  - ▶ whether or not they took HeadacheRelief™ ( $A_i = 1$  or  $A_i = 0$ )
  - ▶ whether or not their headache was relieved within one hour of taking the medication ( $Y_i = 1$  or  $Y_i = 0$ )
- ▶ With the people around you, discuss the following:
  - ▶ Thinking about how treatment is defined here, could there be any potential issues in this study?
  - ▶ How do you interpret “take headache medication”?

# The consistency assumption

- ▶ holds for precise treatments (today)
- ▶ holds with clarity about interference among units (next lecture)

$$\text{If } A_i = a, \text{ then } Y_i^a = Y_i$$

$Y_i^{\text{Treatment}}$

$Y_i^{\text{Control}}$

Potential Outcomes

$Y_i$

Factual Outcomes

# Precise treatments

Imagine you are a high school counselor.

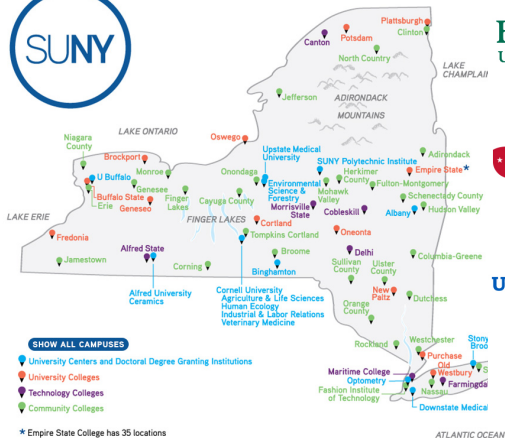
A statistician tells you

The probability of receiving a BA in 6 years would be higher if a student initially enrolled in the State University of New York instead of a community college

$$P\left(\text{BA}^{\text{Enroll in SUNY}}\right) > P\left(\text{BA}^{\text{Enroll in Community College}}\right)$$

How would you advise students?

# Precise treatments



## 6-year graduation rate

**BINGHAMTON**  
UNIVERSITY  
STATE UNIVERSITY OF NEW YORK

83%



**Stony Brook University**

78%



**University at Buffalo**  
The State University of New York

74%



**UNIVERSITY**  
AT ALBANY  
State University of New York

66%

# Precise treatments

The treatment value  
Enroll in SUNY  
is not sufficiently precise

$BA^{\text{Binghamton}} \neq BA^{\text{Stony Brook}}$   
 $\neq BA^{\text{Buffalo}}$   
 $\neq BA^{\text{Albany}}$

To advise the student,  
a precise treatment  
is more helpful

## 6-year graduation rate

 83%

 Stony Brook University 78%

 74%

 66%

# Precise treatments

Consistency assumption:  $Y = Y^A$

More credible when  $A$  is very precise

- ▶ it is clear how to run a hypothetical experiment
- ▶ it is clear how to inform policy

Example:

- ▶ if  $a = \text{SUNY}$ , then  $Y^a$  is vague.  
To which SUNY should you send the student?
- ▶ if  $a = \text{Binghamton}$ , then  $Y^a$  is clearer

## **A good read:**

Hernán, M. 2016.

“[Does water kill? A call for less casual causal inferences.](#)”

Annals of Epidemiology 26(10):674–680.



# Learning goals for today

At the end of class, you will be able to:

1. Explain the challenge of satisfying conditional exchangeability in observational data
2. Explain part one the consistency assumption
  - ▶ Well-defined, precise treatments