## DAGs Review

#### INFO/STSCI/ILRST 3900: Causal Inference

2 Oct 2023

## Agenda

- Reminders and Announcements
- Review: open/closed paths and independence in DAGs
- ► Example from lecture
- Practice with DAGs

## Reminders and Announcements

Peer reviews- make sure to review all you're assigned

- Task 1 is due tomorrow, Oct 3rd by 11:59pm
- In-class assignments:
  - Notify us in advance if you miss a class
  - Otherwise, get one free pass
  - After that, without advance notice, 0 on assignment
- ► You get **5** flex days, use them!
- Office hours:
  - ► Filippo: Monday 11am-12pm in Comstock 1187
  - Shira: Tuesday 3-4pm in Comstock 1187
- Check Ed for announcements and use for HW help!

## Review

How to check if a *path* is **open** or **blocked**:

- $1. \ \mbox{Traverse}$  the path node by node
- 2. If any node is blocked, the entire path is blocked
- 3. If all nodes are open, then entire path is open

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How to check if a *node* is **open** or **blocked**:

- If collider  $(\rightarrow X \leftarrow)$ :
  - Open if it or any of its descendants are in the conditioning set
  - Otherwise it is blocked
- If non-collider  $(\rightarrow X \rightarrow \text{or} \leftarrow X \leftarrow \text{or} \leftarrow X \rightarrow)$ :
  - Blocked if it is in the conditioning set
  - Otherwise it is open

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Two variables are dependent (statistically associated) if there exists an unblocked path between them. They are independent if all paths between them are blocked.

DAGs help us reason about exchangeability

#### Procedure

- 1) List all paths between A to Y
- 2) Cross out the blocked paths
- 3) Exchangeability holds if all remaining paths are causal



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2)  

$$A \to Y \mid A \to Y$$
  
 $A \leftarrow U \to Y \mid A \to U \to Y \mid A \to Y \mid A \to Y$ 

# Practice Identifying Paths

Go through this exercise in groups.



- ► What are the paths from A to Y?
- Determine if each of the paths is causal or non-causal
- Determine whether each node on each path is a collider or non-collider







causal path

 ${ \ = \ \Box \ } { \ }$ 





causal path

non-causal





causal path non-causal

non-causal

 $\langle \Box \rangle$ 





causal path

non-causal

non-causal

non-causal

□ ► 4/6



If we condition on  $L = \emptyset$ , which paths are open? Which paths are blocked?





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If we condition on  $L = \emptyset$ , which paths are open? Which paths are blocked?



5/6



If we condition on  $L = \emptyset$ , which paths are open? Which paths are blocked?



□ ► 5/6



If we condition on  $L = \{Z\}$ , which paths are open? Which paths are blocked?





If we condition on  $L = \{Z\}$ , which paths are open? Which paths are blocked?



Blocked



If we condition on  $L = \{Z\}$ , which paths are open? Which paths are blocked?



 $\ll \square \rightarrow$ 



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